

$$e) \int \left(\pi - \frac{1}{2x} + e^{-2x} \right) dx = \pi x - \frac{1}{2} \ln|x| - \frac{1}{2} e^{-2x} + C$$

$$f) \int \sin^4 x \underbrace{\cos^2 x}_{1-\sin^2 x} \underbrace{\cos x dx}_{d(\sin x)} = \frac{\sin^5 x}{5} - \frac{\sin^7 x}{7} + C$$

$$g) \int \frac{\tan^2 x \cdot \tan x \sec x dx}{\sec^2 x - 1} = \frac{\sec^3 x}{3} - \sec x + C$$

$$h) \int \frac{dx}{\sqrt{(x-2)^2 - 12}} = \ln \left| x-2 + \sqrt{(x-2)^2 - 12} \right| + C$$

$$i) \int \frac{x+3}{4x^2+4x+3} dx = \frac{1}{8} \int \frac{8x+4+20}{4x^2+4x+3} dx = \frac{1}{8} \int \frac{8x+4}{4x^2+4x+3} dx + \frac{20}{8} \int \frac{dx}{(2x+1)^2+2}$$

$$= \frac{1}{8} \ln|4x^2+4x+3| + \frac{20}{8} \cdot \frac{1}{2} \cdot \frac{1}{\sqrt{2}} \operatorname{arctan} \frac{x}{\sqrt{2}} + C$$

$$i) \int x^3 (1+2x^2)^{-3/2} dx = \frac{1}{2} \int \left(\frac{t^2-1}{2} \right) t^{-3} dt$$

$$\Gamma r=3, p=2, q=-3/2$$

$$\frac{r+1}{p} = 2 \in \mathbb{Z}, 1+2x^2 = t^2$$

$$x dx = \frac{1}{2} dt$$

$$= \frac{1}{4} \int (1-t^{-2}) dt = \frac{1}{4} \left(t + \frac{1}{t} \right) + C$$

$$= \frac{1}{4} \left(\sqrt{1+2x^2} + \frac{1}{\sqrt{1+2x^2}} \right) + C$$

$$j) \int \frac{dx}{(x+1)\sqrt{x^2+1}} = \int t \frac{-1/2 t^2 dt}{\sqrt{\left(\frac{1}{t}-1\right)^2+1}} = - \int \frac{dt}{t \sqrt{\frac{1}{t^2} - \frac{2}{t} + 2}}$$

$$\Gamma \frac{1}{x+1} = t, \frac{1}{t} - 1 = x$$

$$dx = -\frac{1}{t^2} dt$$

$$= - \int \frac{dt}{\sqrt{1-2t+2t^2}} = -\frac{1}{\sqrt{2}} \int \frac{dt}{\sqrt{\left(t-\frac{1}{2}\right)^2 + \frac{1}{4}}}$$

$$= -\frac{1}{2} \ln \left| \left(t-\frac{1}{2}\right) + \sqrt{\left(t-\frac{1}{2}\right)^2 + \frac{1}{4}} \right| + C$$

$$= -\frac{1}{2} \ln \left| \frac{1}{x+1} - \frac{1}{2} + \sqrt{\left(\frac{1}{x+1} - \frac{1}{2}\right)^2 + \frac{1}{4}} \right| + C$$